

$$\textcircled{a} \quad f(x) = 2x - 1$$

$$g(x) = -\frac{1}{3}x + 5$$

$$\begin{aligned}(f \circ g)(x) &= f(g(x)) \\ &= f\left(-\frac{1}{3}x + 5\right) \\ &= 2\left(-\frac{1}{3}x + 5\right) - 1 \\ &= -\frac{2}{3}x + 10 - 1\end{aligned}$$

$$\boxed{(f \circ g)(x) = -\frac{2}{3}x + 9}$$

$$\textcircled{b} \quad f(x) = -\frac{3}{7}x + 2$$

$$g(x) = \frac{1}{2}x + \frac{2}{3}$$

$$\begin{aligned}(f \circ g)(x) &= f(g(x)) \\ &= f\left(\frac{1}{2}x + \frac{2}{3}\right) \\ &= -\frac{3}{7}\left(\frac{1}{2}x + \frac{2}{3}\right) + 2 \\ &= -\frac{3}{14}x - \frac{2}{7} + 2\end{aligned}$$

$$\boxed{(f \circ g)(x) = -\frac{3}{14}x + \frac{12}{7}}$$

$$\textcircled{c} \quad f(x) = \frac{2x-1}{3x+5}$$

$$g(x) = \frac{7x+1}{3x-4}$$

$$\begin{aligned}(f \circ g)(x) &= f(g(x)) \\ &= f\left(\frac{7x+1}{3x-4}\right) \\ &= \frac{2\left(\frac{7x+1}{3x-4}\right) - 1}{3\left(\frac{7x+1}{3x-4}\right) + 5} \cdot \frac{(3x-4)}{(3x-4)} \\ &= \frac{2(7x+1) - (3x-4)}{3(7x+1) + 5(3x-4)} \\ &= \frac{14x + 2 - 3x + 4}{21x + 3 + 15x - 20}\end{aligned}$$

$$\boxed{(f \circ g)(x) = \frac{11x + 6}{36x - 17}}$$

$$\textcircled{d} \quad f(x) = 3x + 5$$

$$g(x) = \frac{1}{x+2}$$

$$\begin{aligned}(f \circ g)(x) &= f(g(x)) \\ &= f\left(\frac{1}{x+2}\right) \\ &= 3\left(\frac{1}{x+2}\right) + 5 \\ &= \frac{3}{x+2} + 5 \cdot \frac{(x+2)}{(x+2)} \\ &= \frac{3 + 5(x+2)}{x+2} \\ &= \frac{3 + 5x + 10}{x+2}\end{aligned}$$

$$\boxed{(f \circ g)(x) = \frac{5x + 13}{x+2}}$$